



Attractor? I Hardly Know Her!

featuring rotations and ODEs in VR

2016 Spring MEGL Symposium

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This Semester

- Rotations Demo
- Chaotic Attractors ODE Solver

Rotations

- Exploring IUPUI's Daniel Ramras' paper "How efficiently can one untangle a double-twist? Waving is believing!"
- Nullhomotopy in $SO(3)$
 - Dirac belt trick
 - Philippine candle dance

More formally...

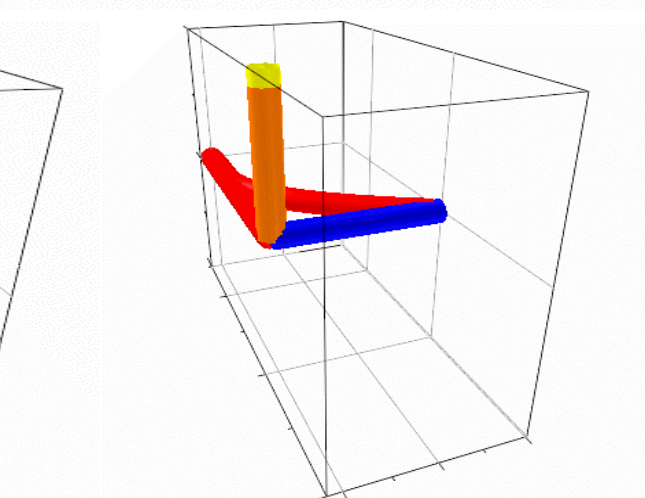
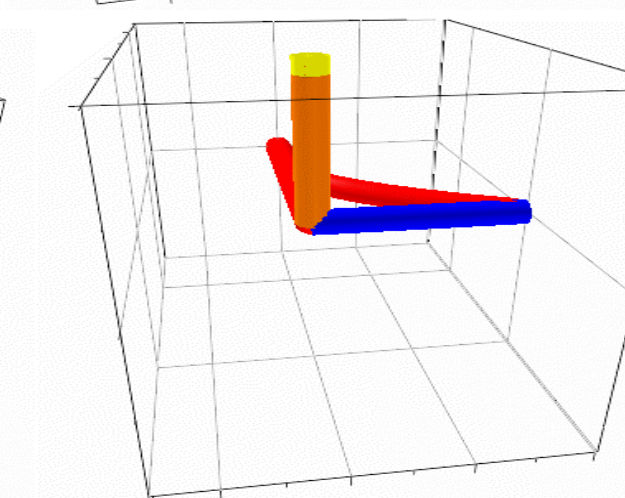
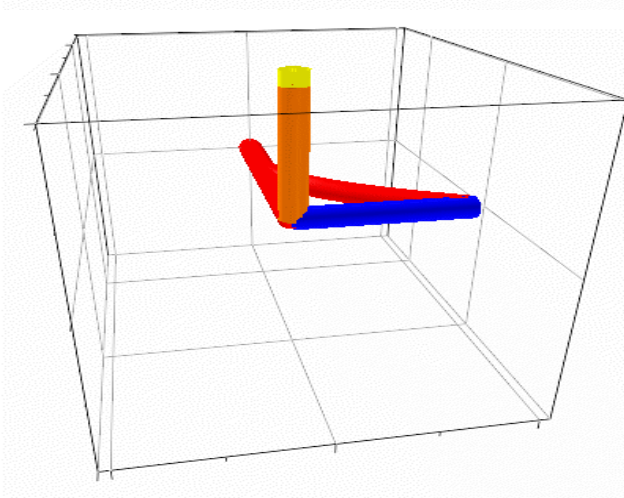
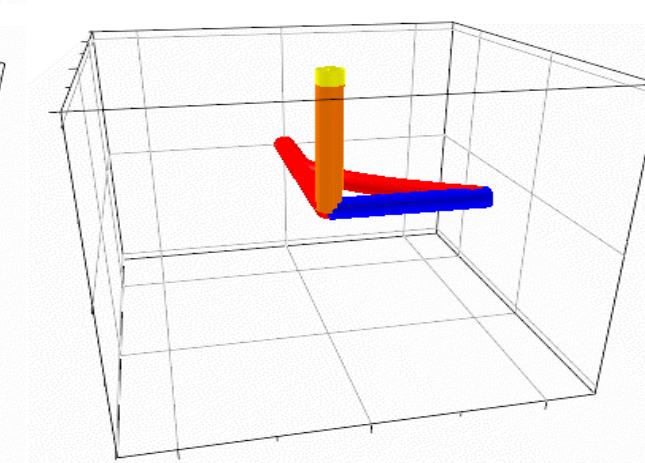
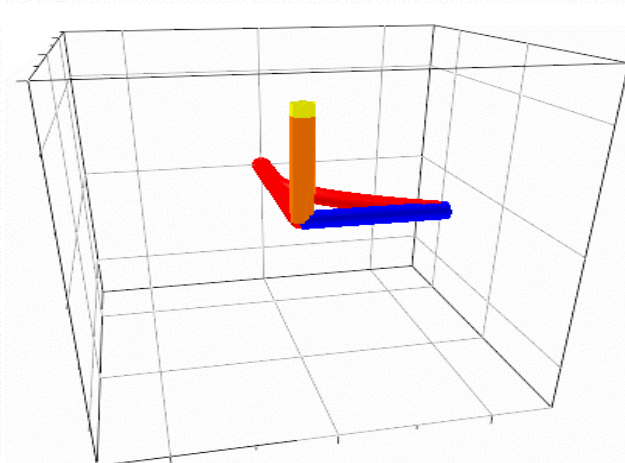
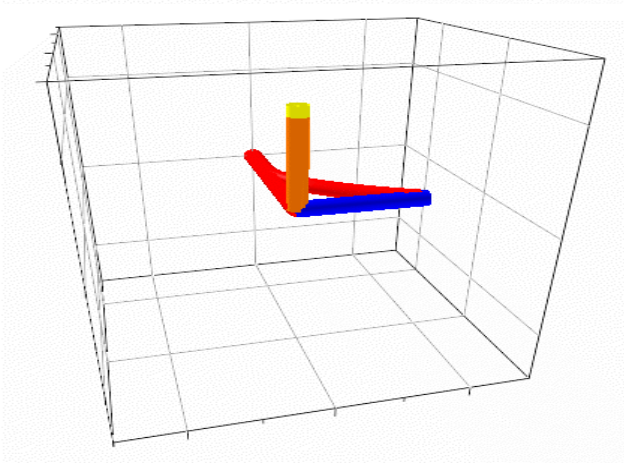
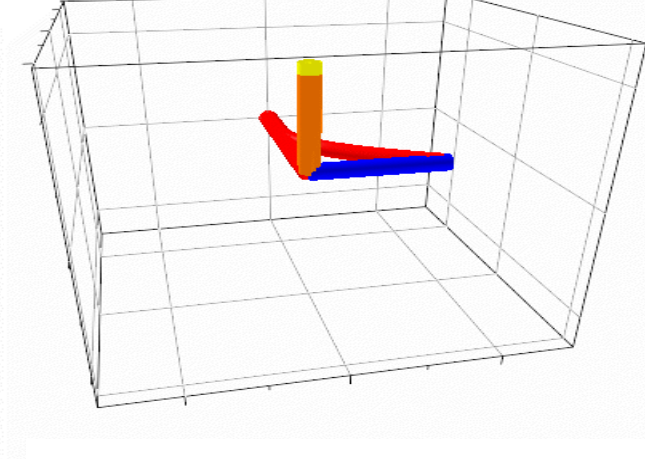
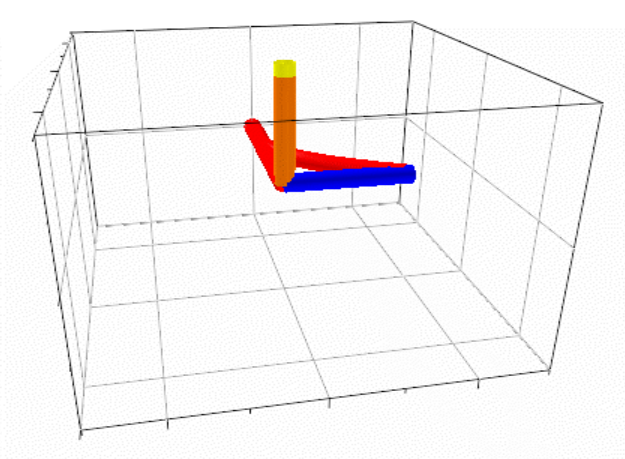
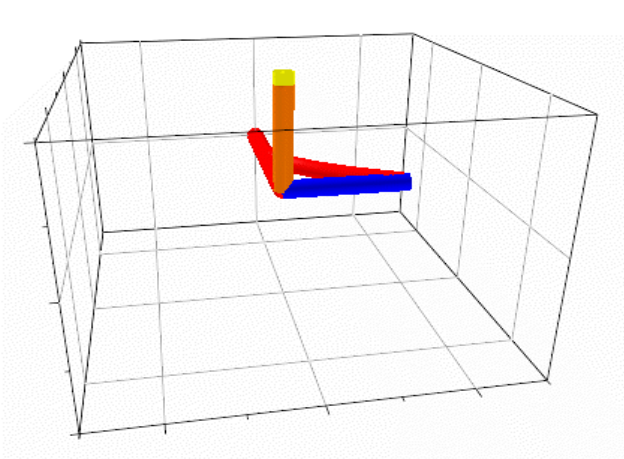
- Double twist can be given by the mapping:

$$\hat{D}(s,t) = (1 - 2 \cos^2 s \sin^2(t/2)) + I(\sin(2s) \sin^2(t/2)) + K(\cos s \sin t)$$

where $0 \leq s \leq \pi/2$ and $0 \leq t \leq 2\pi$

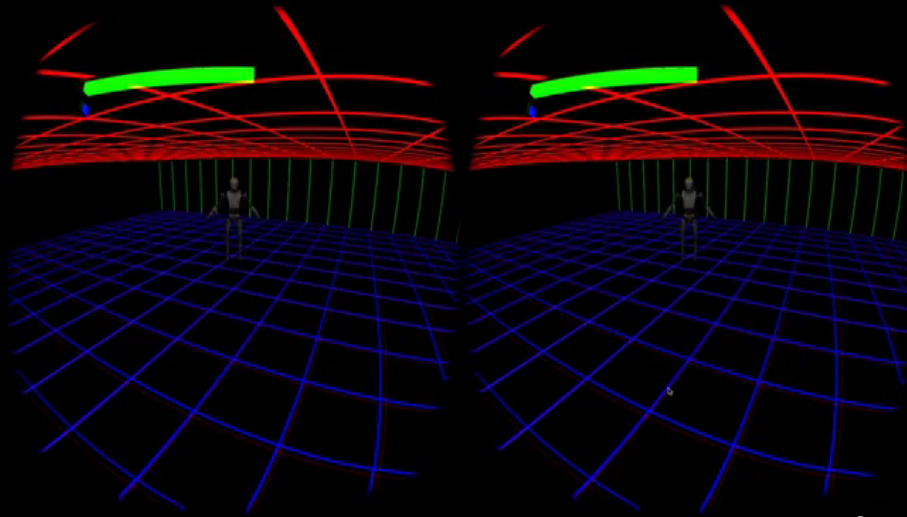
- I??? K???
- Rotations can be conveniently described by *quaternions*
- 4D complex numbers $r + x I + y J + z K$ where

$$I^2 = J^2 = K^2 = IJK = -1$$



Throw Up Simulator (TUS)

- Implemented these rotations in Unity and Oculus Rift

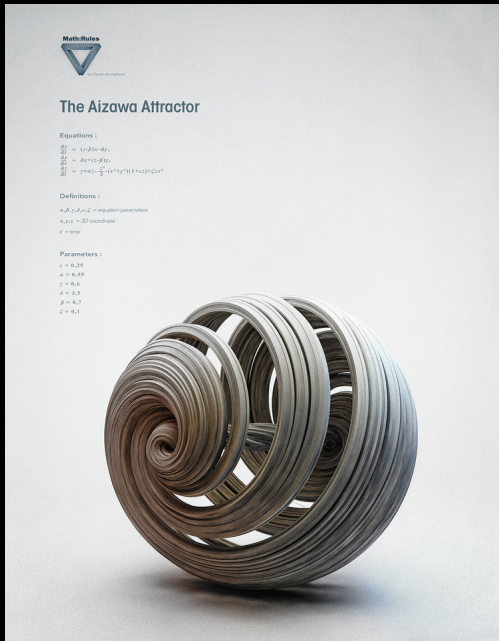


- Feel free to test out your stomachs after the presentation

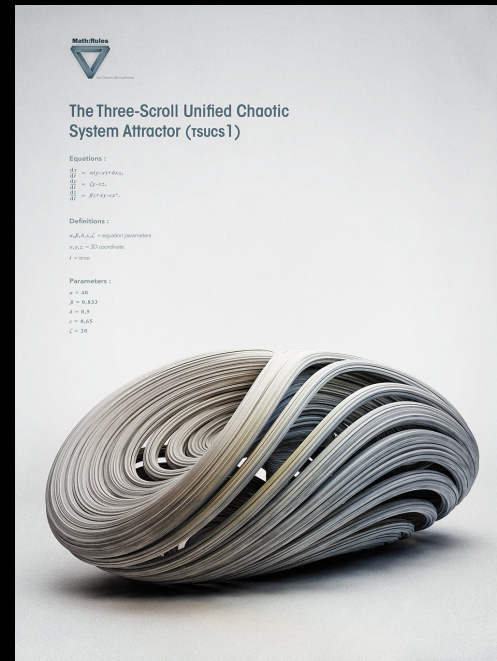
ODE Solver

- Solves ODEs in real time with user-selected initial conditions
 - LEAP motion
- Approximates solutions using a fourth-order Runge-Kutta method
- 15 chaotic attractors
 - Lorenz, Rossler, to name a few

“Strange” Attractors



$$\begin{aligned} \dot{x} &= (z - \beta)x - dy \\ \dot{y} &= \delta x + (z - \beta)y \\ \dot{z} &= \gamma + \alpha z - \frac{z^3}{3} - (x^2 + y^2)(1 + \varepsilon z) + \xi z x^3 \end{aligned}$$



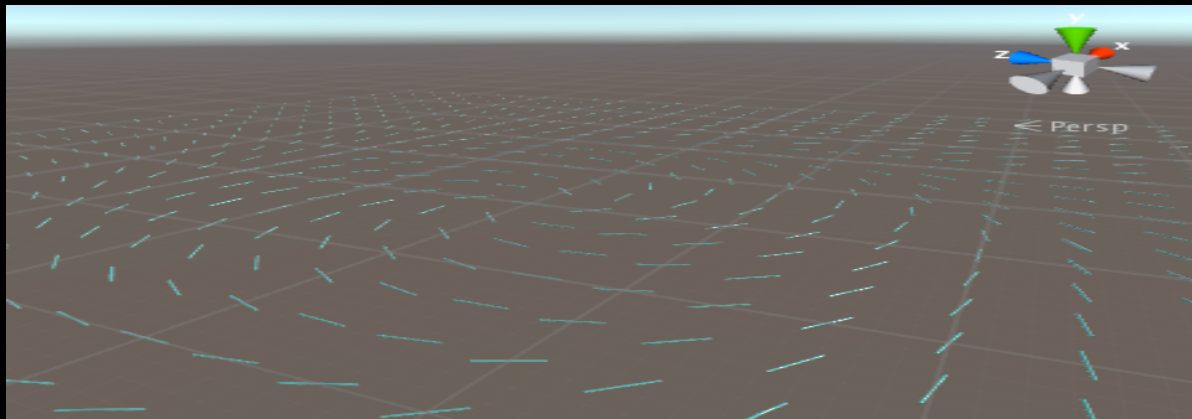
$$\begin{aligned} \dot{x} &= \alpha(y - x) + \delta x z \\ \dot{y} &= \zeta y - x z \\ \dot{z} &= \beta z + x y - \varepsilon x^2 \end{aligned}$$

ODE Footage



Future Plans

- Turn ODE solver into outreach carnival game
 - Attractor golf





Future Plans

- Moduli spaces with Jack Love
- Hyperbolic geometry?



Acknowledgments

- Thank you to our advisor, Dr. Sean Lawton
- MEGL
- NSF

Stick around to experience the Rift

